

Particles and Waves (10 points)

Part A. Quantum particle in a box (1.4 points)

A.1 (0.4 pt)

$$E_{\min} =$$

A.2 (0.6 pt)

$$E_n =$$

A.3 (0.4 pt)

$$\lambda_{21} =$$

Part B. Optical properties of molecules (2.1 points)

B.1 (0.8 pt)

Expression: $\lambda =$

Numerical value: $\lambda \approx$

B.2 (0.4 pt)

Absorption spectrum of Cy3 is shifted to (check): ☐ bluer ☐ redder
spectral region by $\Delta\lambda \approx$

B.3 (0.7 pt)

$$K =$$

B.4 (0.2 pt)

Numerical value: $\tau_{\text{Cy5}} \approx$

Part C. Bose-Einstein condensation (1.5 points)

C.1 (0.4 pt)

$$p =$$

$$\lambda_{\text{dB}} =$$

C.2 (0.5 pt)

$$\ell =$$

$$T_c =$$

C.3 (0.6 pt)

Expression: $n_c =$

Numerical value: $n_c \approx$

Expression: $n_0 =$

Numerical value: $n_0/n_c \approx$

Part D. Three-beam optical lattices (5 points)

D.1 (1.4 pt)

$$V(\vec{r}) =$$

$$\vec{b}_1 =$$

$$\vec{b}_2 =$$

$$\vec{b}_3 =$$

D.2 (0.5 pt)

Argument:

D.3 (1.2 pt)

$V_X(x) =$

$V_Y(y) =$

Minimum (-a) of $V_X(x)$: at $x =$

Maximum (-a) of $V_X(x)$: at $x =$

Minimum (-a) of $V_Y(y)$: at $y =$

Maximum (-a) of $V_Y(y)$: at $y =$

D.4 (0.8 pt)

Ratio of the lattice constant to the laser wavelength: $a/\lambda_{\text{las}} =$

Positions of all equivalent minima nearest to the origin:

D.5 (1.1 pt)

Expression: $n =$

Numerical value: $n \approx$