

Theoretical Question 1: Particles and Waves**MARKING SCHEME**

Total	Mark(s)	Marking Scheme for Answers
Part A 4.0	(a) 1.1	<p>(i) Q in terms of m, M, p_1, p_{2x}, and p_{2y}.</p> <ul style="list-style-type: none"> ➤ 0.2 for expression of Q → (a-2)† <p>(ii) Plot of condition relating p_1, p_{2x}, and p_{2y}.</p> <ul style="list-style-type: none"> ➤ 0.2 for circle and the position of its center ➤ 0.1 for intersection point $(m - M)p_1/(m + M)$ → (a-3) ➤ 0.1 for intersection point p_1 → (a-3) ➤ 0.3 for labeling regions for $Q = 0, Q > 0$, and $Q < 0$ (0.1 each) <p>Allowed regions of Q.</p> <ul style="list-style-type: none"> ➤ 0.2 for allowed regions: $Q > 0$ and $Q = 0$ (0.1 each)
	(b) 2.9	<p>(i) Equation relating x to $Q, \theta, d_0, m, k, M, p_1$ and p_2.</p> <ul style="list-style-type: none"> ➤ 0.2 for correctly stating the energy conservation → (a-5) ➤ 0.2 for correct rotational energy expression → (a-6) ➤ 0.3 for expression of Q → (a-7) <p>(ii) Threshold value p_c in terms of m, M, and p_1.</p> <ul style="list-style-type: none"> ➤ 0.3 for $\alpha_{\min} = 0$ ➤ 0.4 for α_{\max} → (a-12) ➤ 0.4 for expression of p_c. → (a-13) <p>Sketch of σ versus p_2.</p> <ul style="list-style-type: none"> ➤ 0.4 for σ increasing with p_2 quasi-linearly and becoming level beyond p_c →(a-14) ➤ 0.4 for range of p_2 →(a-9) ➤ 0.3 for range of $\sigma = (0,1)$
Part B 3.0	(c) 2.2	<p>Period of vibration T.</p> <ul style="list-style-type: none"> ➤ 0.5 for $T = 2L/c$ →(b-4) <p>Shape of the string at $t = T/8$.</p> <ul style="list-style-type: none"> ➤ 0.5 for decomposing the triangle into two traveling waves ➤ 0.5 for correct shape →(b-5) ➤ 0.3 for correct lengths $L/4, L/2$ and $L/4$ ➤ 0.2 for correct height $h/2$ ➤ 0.2 for $\tan\theta = 2h/L$

	(d) 0.8	<p>The total mechanical energy E.</p> <p>➤ 0.4 for expression of $E = 2\mu h^2 c^2 / L$ (for all cases below) →(b-7)</p> <p>For the remaining 0.4 point:</p> <p>case 1: calculating the work done by normal force</p> <p>➤ 0.2 for correct expression of the normal force →(b-6)</p> <p>➤ 0.2 for correct relation of E to the normal force</p> <p style="text-align: center;">or</p> <p>case 2: calculating the potential energy</p> <p>➤ 0.4 for correct form of the potential energy →(b-7')</p> <p style="text-align: center;">or</p> <p>case 3: calculating the kinetic energy</p> <p>➤ 0.4 for calculating velocity correctly →(b-7'')</p>
Part C 3.0	(e) 2.2	<p>Distance (in units of Mpc) of the star from us.</p> <p>➤ 1.0 for $L(t_e) = \int_{t_e}^{t_0} \frac{a(t_e)}{a(t)} c dt$ →(c-3)</p> <p>➤ 0.5 for $L(t_e) = \frac{c}{H} (1 - \exp[-H(t_e - t_0)])$ →(c-3)</p> <p>➤ 0.4 for $\exp[-H(t_0 - t_e)] \approx 1.200$ →(c-4)</p> <p>➤ 0.3 for value of $L(t_e) \approx 690$ Mpc →(c-5)</p>
	(f) 0.8	<p>The receding velocity (in units of c) of the star.</p> <p>➤ 0.3 for $L(t_0) = \frac{a(t_0)}{a(t_e)} L(t_e)$ or $L(t_0) = \frac{\lambda(t_0)}{\lambda(t_e)} L(t_e)$ →(c-5)</p> <p>➤ 0.2 for expression of $v(t_0)$ →(c-7)</p> <p>➤ 0.3 for value of $v(t_0) \approx 0.200 c$ →(c-7)</p>

†The equation number(s) at the end of a line refers to equation(s) in the SOLUTION sheets.