## [Marking Scheme] Theor

## Theoretical Question 1

## When will the Moon become a Synchronous Satellite?

(1)	0.4	<i>location</i> of center of mass C
		$\succ$ 0.2 for distance to Earth
3.0		0.2 for distance to Moon
	0.4	<i>Orbital</i> angular momentum of the <i>Moon</i> $\ell_M$
		$\succ$ 0.2 for formula
		➢ 0.2 for numerical value
	0.4	<i>spin</i> angular momentum of the <i>Moon</i> $S_M$
		$\succ$ 0.2 for formula
		0.2 for numerical value
	0.4	<i>Orbital</i> angular momentum of the <i>Earth</i> $\ell_E$
		$\succ$ 0.2 for formula
		➢ 0.2 for numerical value
	0.4	<i>spin</i> angular momentum of the <i>Earth</i> $S_E$
		$\succ$ 0.2 for formula
		➤ 0.2 for numerical value
	0.2	knowing total angular momentum of a system is the sum of
		orbital and spin angular momenta
	0.8	<i>total</i> angular momentum of the Earth-Moon system L
		0.2 for order of magnitude
		0.4 for value to two significant digits
	0.0	➤ 0.2for unit
(2)	0.8	Newton's form of <i>Kepler's third law</i> $\omega^2 r^3 = G(M_E + M)$
3.0		→ 0.6 for $\omega^2 r^3$ = constant
		> 0.2 for expression of constant $G(M_E + M)$
	0.4	realizing total orbital angular momentum $\ell = \ell_E + \ell_M$ is a
		function of $\omega$ or alone
	0.2	realizing spin angular momentum of the Moon is negligible
	0.4	resorting to the law of conservation of total angular momentum
	1.2	<i>period of rotation</i> of the Earth <i>T</i>
		$\triangleright$ 0.3 for order of magnitude in units of second
		0.4 for value to two significant digits
(		$\triangleright$ 0.5 for providing an equation for finding T
(3)	0.2	0.2 for knowing $\Gamma = (\frac{r_0}{r})^6 \Gamma_0$
4.0	0.4	realizing relation between torque and rate of slowdown of Earth's
		rotation: $dS_F / dt = \Gamma$
	0.4	concluding - $\Gamma$ is equal to rate of increase of <i>total orbital angular</i>
		<i>momentum</i> of the Earth-Moon system: $d\ell/dt = -\Gamma$
	1.0	<i>current value</i> of the <i>torque</i> $\Gamma_0$
		> 0.2 for realizing $\ell$ is related to r
		> 0.3 for converting the derivative $d\ell/dt$ to $dr/dt$

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	> 0.4 for value of $\Gamma_0$
	➢ 0.1 for unit of torque
0.6	converting the derivative $d\ell/dt$ to $d\omega/dt$
	> 0.1 for realizing $\ell$ is related to $\omega$
	> 0.1 for realizing $\Gamma$ is related to $\omega$
	> 0.4 for converting $d\ell/dt = -\Gamma$ into a differential equation
	for $\omega$
0.6	<i>providing</i> an <i>equation</i> for the solution of $t_f$
0.8	estimate of time $t_f$
	> 0.3 for order of magnitude in units of second
	0.4 for value to two significant digits
	▶ 0.1 for value in years